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ME 323 MIDTERM EXAM 2 Spring 2011 8:00 PM – 9:00 PM

Instructions

- 1. Work each problem in the space provided.
- 2. Confine your work to the front side of the pages only.
- 3. Additional paper will be provided upon request.
- 4. Each problem is of equal value.
- 5. To obtain maximum credit for a problem, you must present your solution clearly. Accordingly:
 - a. Identify coordinate systems
 - b. Sketch free body diagrams
 - c. State units explicitly
 - d. Clarify your approach to the problem including assumptions
 - e. Clearly mark final answers with boxes
- 6. If your solution cannot be followed, it will be assumed that it is in error.

| | | \backslash |
|-------|-----|--------------|
| Prob | . 1 | |
| Prob | . 2 | |
| Prob | . 3 | |
| Total | | |

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Some useful formulas

$$\varepsilon_{x} = \frac{1}{E} \left[\sigma_{x} - \nu \left(\sigma_{y} + \sigma_{z} \right) \right] + \alpha \Delta T$$

$$\varepsilon_{y} = \frac{1}{E} \left[\sigma_{y} - \nu \left(\sigma_{x} + \sigma_{z} \right) \right] + \alpha \Delta T$$

$$\varepsilon_{z} = \frac{1}{E} \left[\sigma_{z} - \nu \left(\sigma_{x} + \sigma_{y} \right) \right] + \alpha \Delta T$$

$$\gamma_{xy} = \frac{1}{G} \tau_{xy} \quad \gamma_{xz} = \frac{1}{G} \tau_{xz} \quad \gamma_{yz} = \frac{1}{G} \tau_{yz}$$

$$\sigma = -\frac{My}{I}$$

$$\tau = \frac{VQ}{It}; \quad Q = A'\overline{y}'$$

$$I_{\text{rectangle}} = \frac{1}{12}bh^{3}$$

$$I_{\text{circle}} = \frac{\pi}{4}r^{4}$$

Centroid of a semicicle = $\overline{y} = \frac{4r}{3\pi}$

$$\sigma_{a} = \frac{pr}{2t}$$
$$\sigma_{h} = \frac{pr}{t}$$
$$\sigma_{sphere} = \frac{pr}{2t}$$

$$e = \frac{FL}{EA} + L\alpha\Delta T$$

$$\tau = \frac{T\rho}{J}$$

$$\tau = G\frac{\phi r}{L}$$

$$\phi = \frac{TL}{GJ}$$

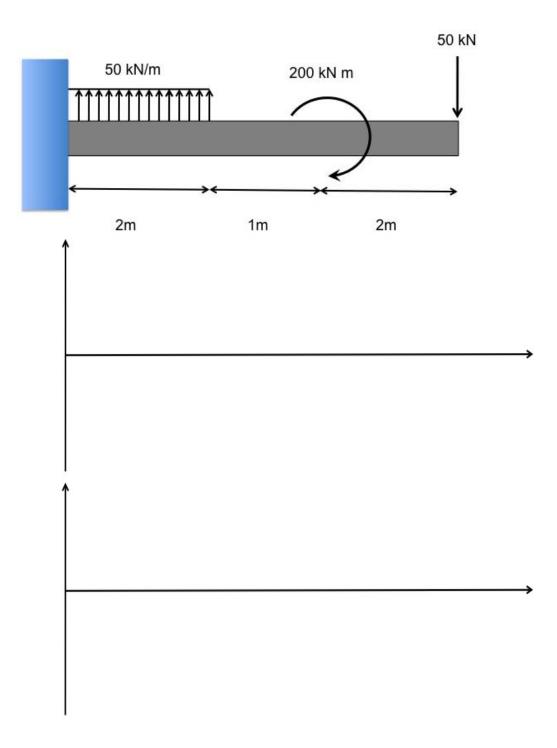
$$J_{solid} = \frac{\pi d^4}{32}$$

$$J_{hollow} = \frac{\pi (d_o^4 - d_i^4)}{32}$$

 $FS = \frac{Failure \ Stress}{Allowable \ Stress}$

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PROBLEM #1 (35 points) Construct the shear and bending moment diagrams. Clearly write all the information in the diagrams (only the diagrams will be graded).



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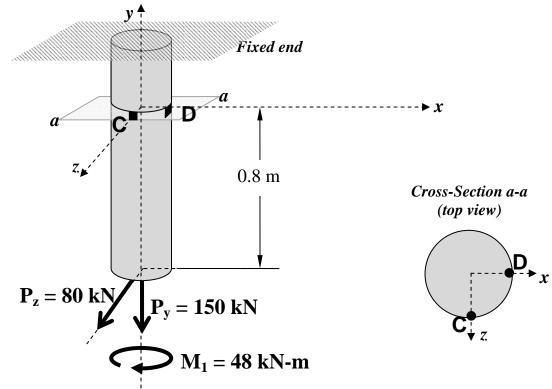
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PROBLEM #2 (35 points)

Given:

Two point forces and a moment were applied on a solid rod ($\underline{radius = 0.1 m}$), as shown in the diagram. The force $\mathbf{P_y} = 150$ kN acted along the rod's axis (in -y direction), the force $\mathbf{P_z} = 80$ kN acted in the +z direction, and the moment $\mathbf{M_1} = 48$ kN-m acted in the -y direction. Neglect the effect of gravity.



Find:

- a) The internal resultants acting on the surface a-a
- b) The state of stress at point **C** (show in a stress element with coordinate system)
- c) The state of stress at point **D** (show in a stress element with coordinate system)

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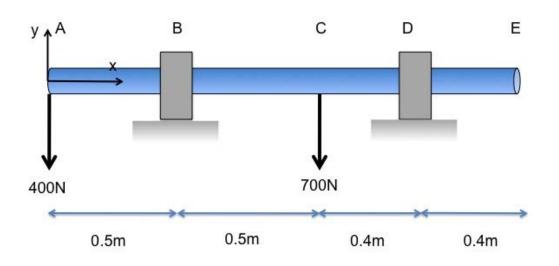
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PROBLEM #3 (30 points)

A solid steel shaft with 10 cm radius supports the loads shown in the figure. The bearings at B and D are roller supports.

(a) Find the magnitude and location (x and y coordinates) of the maximum shear stress in the shaft.



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